

Unit G

Constructions

(Geometer's Sketchpad)



Name: _____

Constructions Unit - Geometer's Sketchpad

Directions: Use the steps to construct the following figures using Geometer's Sketchpad. Do not move on until your teacher has initialed the previous construction.

#1: Copy a segment

- 1) Construct \overline{AB} . This is your given segment.
- 2) Construct point C not on \overline{AB} . This is one endpoint of your new segment.
- 3) Select \overline{AB} and C and choose *Circle By Center+Radius* in the *Construct* Menu.
- 4) Construct \overline{CD} , where D is on the circle.
- 5) Hide the circle

Teacher's Initials _____

Investigate

Move points C and D. Do they behave as you would expect them to? Move point A or B. What effect does changing the length of \overline{AB} have on \overline{CD} ?

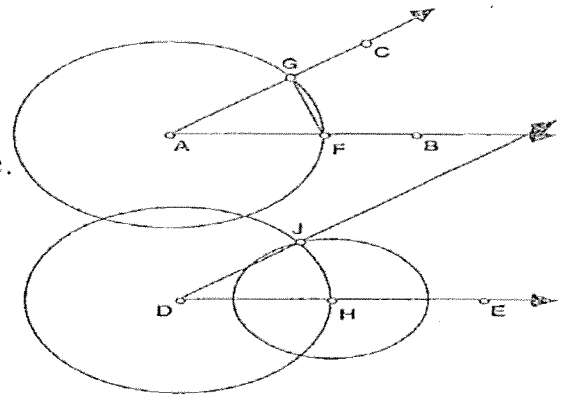
#2: Construct a line parallel to a given line through a point not on the line

- 1) Construct \overline{AB} and point C, not on \overline{AB} .
- 2) Select \overline{AB} and point C, and *construct* a parallel line.

Teacher's Initials _____

#3: Copy an angle

- 1) Construct rays \overline{AB} and \overline{AC} . This is your given angle.
- 2) Construct \overline{DE} . This is one side of a new angle.
- 3) Construct point F on \overline{AB} . Then construct segment \overline{AF}
- 4) Construct circle AF by selecting point A and segment \overline{AF} , and then choosing *Circle by Center+Radius* from the *Construct* menu.
- 5) Construct \overline{FG} , where G is the point of intersection of the circle and \overline{AC} .
- 6) Construct a circle with center D and radius AF.
- 7) Construct H, the point of intersection of this circle with \overline{DE} .
- 8) Construct a circle with center H and radius FG.
- 9) Construct \overline{DJ} , where J is the point of intersection of these two circles.



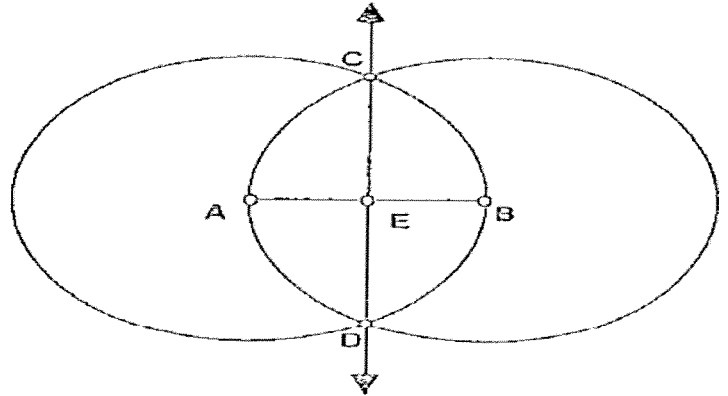
Teacher's Initials _____

Investigate

Move points A, B, C, D, or E. Do the angles remain congruent? When you drag J, why doesn't $\angle JDH$ change?

#4: Constructing perpendicular lines & the bisector of a segment

- 1) Construct segment \overline{AB} .
- 2) Select \overline{AB} and A and choose *Circle By Center+Radius* in the *Construct* Menu.
- 3) Select \overline{AB} and B and choose *Circle By Center+Radius* in the *Construct* Menu.
- 4) Construct \overline{CD} , where C and D are the points of intersection of the circles.
- 5) Construct E, the point of intersection of \overline{AB} and \overline{CD} .
- 6) Hide the circles.



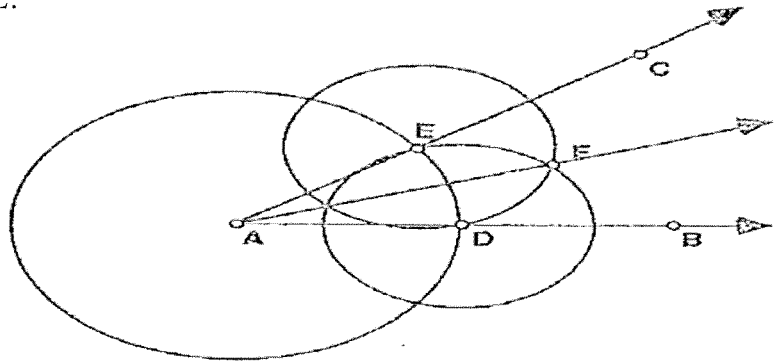
Teacher's Initials _____

Investigate

\overline{CD} is the perpendicular bisector of \overline{AB} . Move points A and B. What's special about point E?

#5: Bisect an angle

- 1) Construct rays \overrightarrow{AB} and \overrightarrow{AC} .
- 2) Construct point D, a point on \overrightarrow{AB} .
- 3) Construct circle AD by selecting points A and D (in that order) and choosing *Circle By Center+Point* in the *Construct* Menu.
- 4) Construct point E at the intersection of \overrightarrow{AC} and the circle created above.
- 5) Construct circles DE and ED. (*Hint: Refer to step 3 above!*)
- 6) Construct \overrightarrow{AF} , where F is the intersection of circles DE and ED that is farthest from A.
- 7) Hide the circles and points D and E.



Teacher's Initials _____

Investigate

Drag point B or C. Does \overrightarrow{AF} continue to bisect the angle?

#6: Construct a square inscribed in a circle

- 1) *Construct* circle AB.
- 2) *Construct* line \overline{AB} .
- 3) Select point A and \overline{AB} , then *construct* a perpendicular line.
- 4) Label the points where the lines meet the circle C, D, and E.
- 5) *Construct* line segments \overline{BC} , \overline{CD} , \overline{DE} and \overline{EB} .
- 6) Hide the circle and the perpendicular lines.

Teacher's Initials _____

Investigate

Drag point B. What happens to the rest of the square? Do the properties of a square remain true?

#7: Construct the circumscribed circles of a triangle

- 1) *Construct* a triangle and label the vertices A, B, and C.
- 2) Select points A and B, then *construct* midpoint.
- 3) Repeat step 2 for the other two sides of the triangle.
- 4) *Label* the midpoints D, E, and F.
- 5) *Construct* lines perpendicular to each side of the triangle through their midpoint.
- 6) *Label* the point of intersection of the three lines G. (*Hint: Select two of the lines, then choose Intersection from the Construct menu*)
- 7) Construct circle GA using *Circle By Center+Point* in the *Construct* Menu.
- 8) Construct circle GB using *Circle By Center+Point* in the *Construct* Menu.
- 9) Construct circle GC using *Circle By Center+Point* in the *Construct* Menu.

Teacher's Initials _____

Investigate

What do you notice about the circles created in steps 7 through 9? What would happen if your triangle was equilateral?

#8: Construct an equilateral triangle inscribed in a circle

- 1) *Construct* a circle.
- 2) *Construct* a segment from the center to a point on the circle to represent the radius.
- 3) With the selection tool, highlight the radius and the point of intersection with the circle. Then **DOUBLE CLICK** the center of the circle. There should be a flash of circles around the center.
- 4) From the menu bar, select the *Transform* option and choose *Rotate*.
- 5) Enter 120 degrees in the box for the rotation. This will create another segment, 120 degrees around the circle.
- 6) Highlight the new segment as done in step 3, and repeat the procedure.
- 7) Connect the three points on the circle with segments.
- 8) Hide the circle.

Teacher's Initials _____

Investigate

Why does rotating the segments work? Can this process be replicated to create other regular polygons?

#9: Construct a regular hexagon inscribed in a circle

- 1) *Construct* a circle.
- 2) *Construct* a segment from the center to a point on the circle to represent the radius.
- 3) With the selection tool, highlight the radius and the point of intersection with the circle. Then **DOUBLE CLICK** the center of the circle. There should be a flash of circles around the center.
- 4) From the menu bar, select the ***Transform*** option and choose ***Rotate***.
- 5) Enter 60 degrees in the box for the rotation. This will create another segment, 60 degrees around the circle.
- 6) Highlight the new segment as done in step 3, and repeat the procedure until you have created six points on the circle.
- 7) Connect the six points on the circle with segments.
- 8) Hide the circle.

Teacher's Initials _____

Investigate

Why did rotating 60 degrees work in making a regular hexagon?

#10: Construct the inscribed circle in a triangle

- 1) *Construct* a triangle. Name it ABC
- 2) *Construct* the bisector of $\angle B$ by selecting points A, B and C (in that order) and choosing *Angle Bisector* from the construct menu.
- 3) Repeat steps 2 and 3 for $\angle A$.
- 4) Label the point of intersection D.
- 5) Construct the bisector of $\angle C$ using the same procedure as above.
- 6) Label the point where the line from step 6 meets the opposite side. Call it E.
- 7) Construct circle DE.

Teacher's Initials _____

Investigate

What do you notice about the inscribed circle? What happens when you move one of the vertices of the original triangle?
