

Name: \_\_\_\_\_

Hour: \_\_\_\_\_

# Chapter 3

## Linear Functions

If I have 10 chocolate cakes and someone asks me for one, how many chocolate cakes do I have left? That's right, 10.



your  cards  
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## Lesson 3-1: Linear Function Intro & Constant-Increase & Constant-Decrease Situations

### Vocabulary

Linear Equation: \_\_\_\_\_  
\_\_\_\_\_

- Requirements:
- Variables must be in \_\_\_\_\_ terms
  - Variables cannot be located in the \_\_\_\_\_
  - Variables cannot have \_\_\_\_\_

### Linear Equations: Important Information

- A solution to a linear equation is a pair of numbers written as a \_\_\_\_\_
- There are \_\_\_\_\_ solutions to a linear equation
- When solutions are graphed, the points form a \_\_\_\_\_
- Linear equations can always be written in \_\_\_\_\_

**Slope-Intercept Form** (remember this is just ONE way to write a linear equation, but there are other ways as well!)



- Slope = a measure of a line's \_\_\_\_\_
- y-intercept = the point where a line cross the \_\_\_\_\_ on a graph

### Constant-Increase or Constant-Decrease Situations

- can be represented with a \_\_\_\_\_
- two parts: initial value = \_\_\_\_\_ & rate of change = \_\_\_\_\_

## Practice

1. Identify the equations that are considered linear equations.

$$y = 3x + 1$$

$$2x + 3y = 9$$

$$y = 2x^2 + 7$$

$$4xy = 11$$

$$\frac{7}{x} = y$$

$$y = 12$$

2. Find three solutions to the linear equation:  $y = 3x - 2$ .

3. Identify the slope & y-intercept of each linear equation.

A.  $y = \frac{2}{3}x - 5$

B.  $y = 2 - 4x$

Slope =

Slope =

y-intercept =

y-intercept =

4. An empty crate weighs 3 kilograms. It is filled with oranges that each weigh 0.2kg.

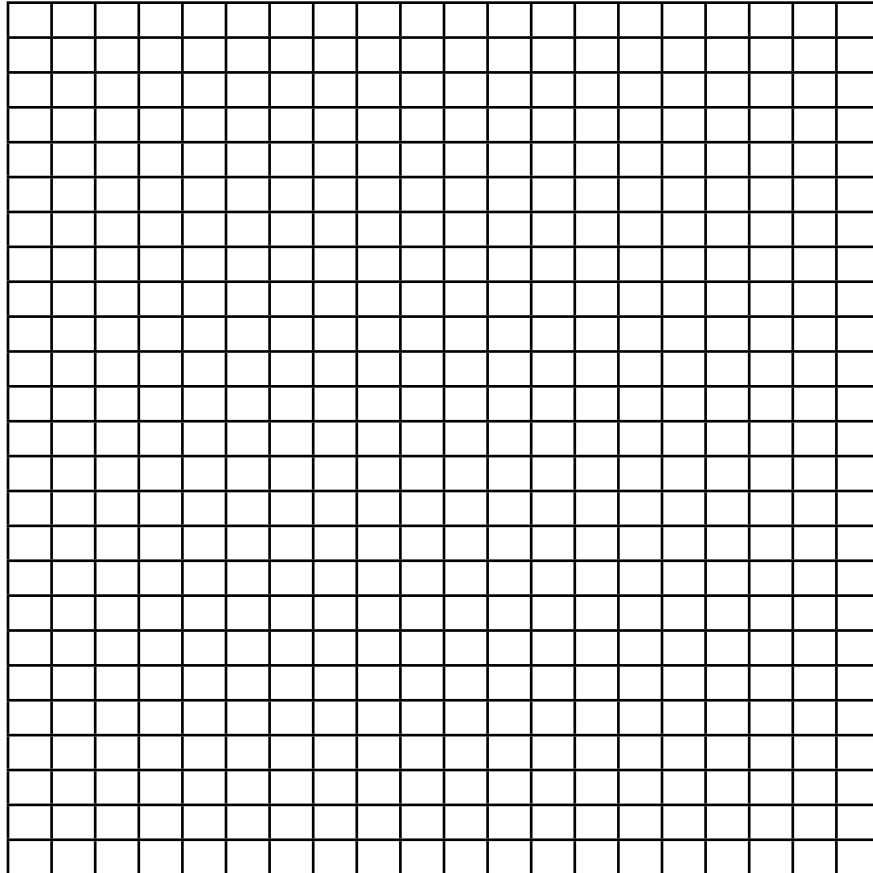
A. Is this a constant-increase or constant-decrease situation?

B. Identify the initial value and rate of change.

C. Write as a linear function.

5. At the beginning of the month, Katie bought a 50 lb sack of wild bird feed. She puts  $\frac{2}{3}$  of a pound into the feeder each morning. Let  $y$  represent the amount of remaining feed after  $x$  days. Write a linear equation relating  $x$  and  $y$ .

6. Al's temperature at 4:00pm was  $99.5^{\circ}$ . It rose at a steady rate of  $0.3^{\circ}$  per hour for 6 hours. Then it stayed constant for four hours. Then, it fell steadily by  $0.4^{\circ}$  per hour for four hours. Make a graph to represent the situation.



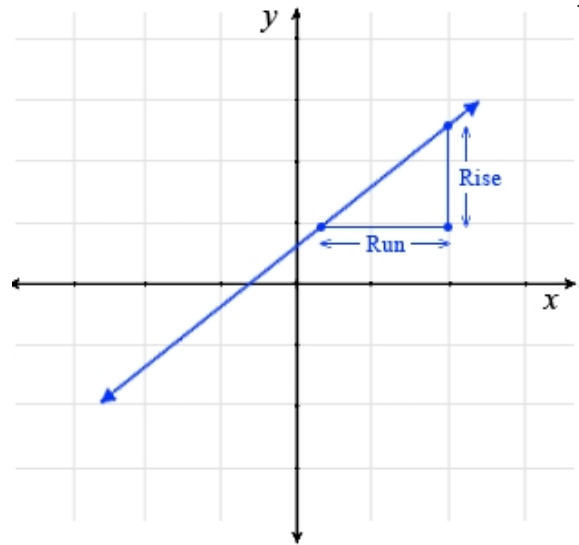
## Lesson 3-2: The Graph of $y = mx + b$

### Vocabulary

Slope: \_\_\_\_\_

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Slope = \_\_\_\_\_



Parallel Lines: \_\_\_\_\_

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Example:

Perpendicular Lines: \_\_\_\_\_

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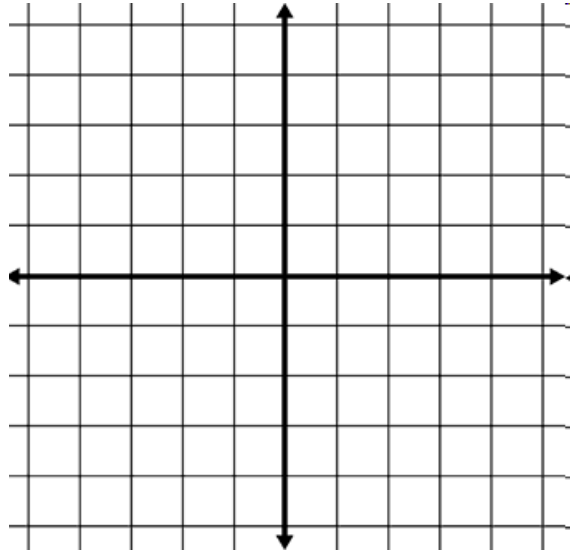
Example:

## Practice

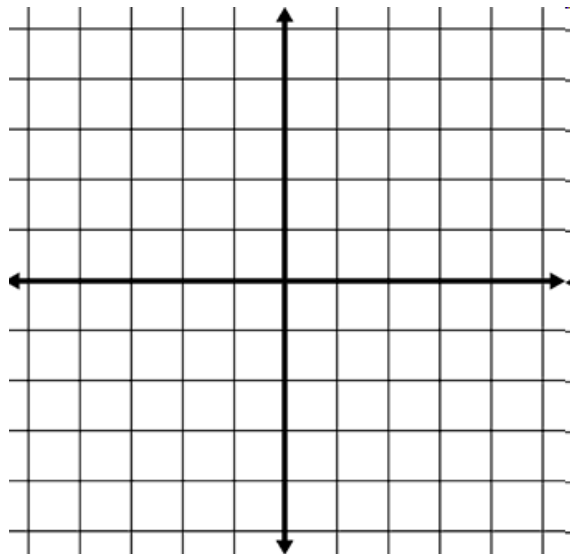
1. Graph the line  $y = 2x - 3$ .

**STEPS:**

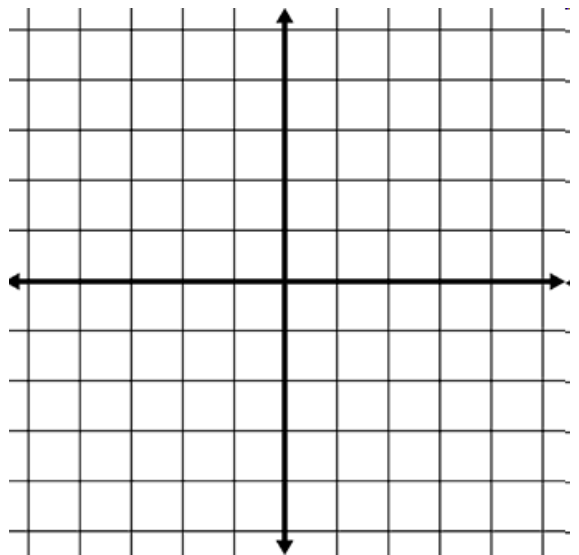
1. Get “y” alone first!
2. Start by plotting the y-intercept.
3. Convert the slope to a fraction.
4. Use the “rise” & the “run” to plot the next few points.
5. Connect the points w/ a straight line.



2. Graph the line  $y = -\frac{1}{2}x + 3$ .

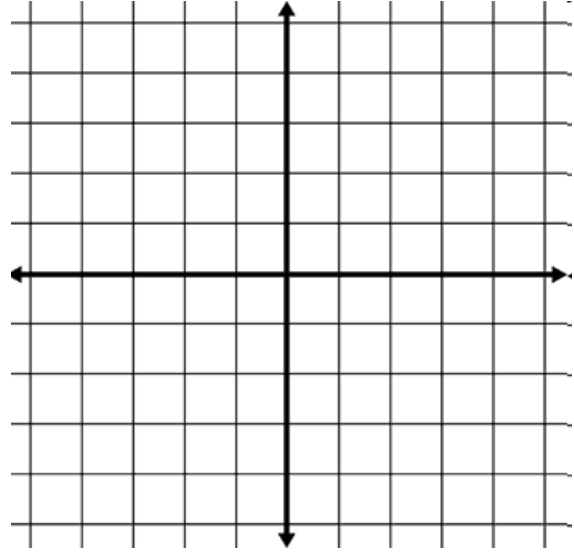


3. Graph the line  $2y = -3x + 8$ .

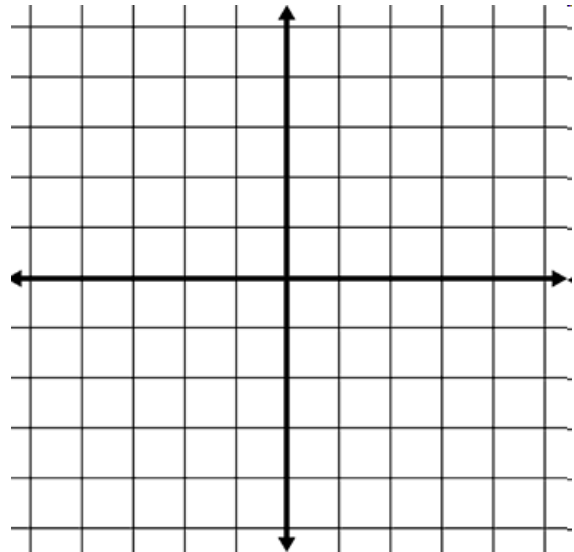


## Weird Cases...

4. Graph the line  $y = 4$ .



5. Graph the equation  $x = -2$ .



## Looking at the weird cases...

Example 4 shows a \_\_\_\_\_.

- Any equation in the form \_\_\_\_\_ will be a horizontal line.
- These lines have a slope of \_\_\_\_\_.

Example 5 shows a \_\_\_\_\_.

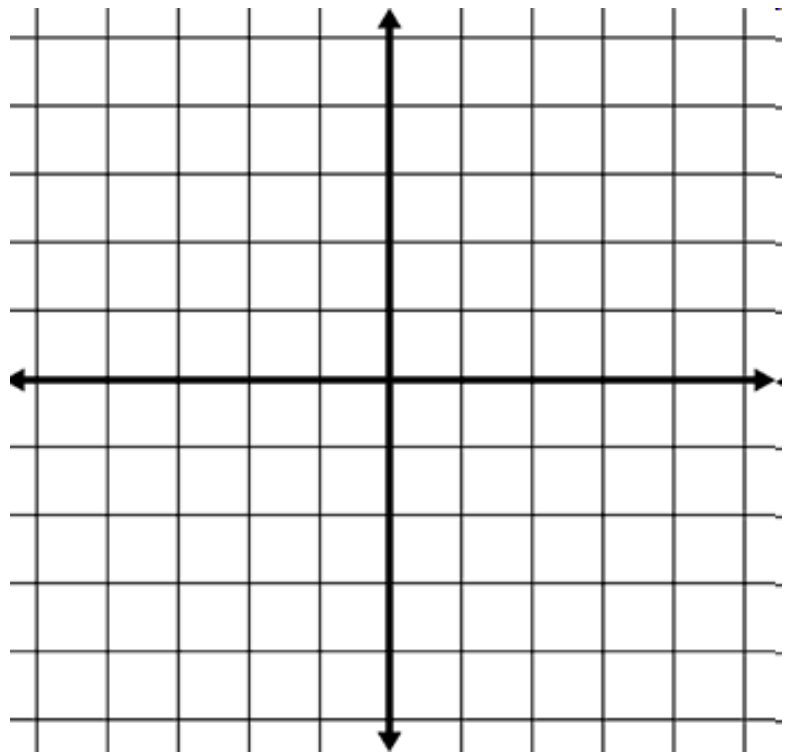
- Any equation in the form \_\_\_\_\_ will be a vertical line.
- These lines have an \_\_\_\_\_ slope.

6. Graph both lines on the same graph.

$$y = -2x + 3$$

$$y = -2x - 2$$

What do you notice???



7. Consider the equation  $y = 3x - 5$ .

- A. Write an equation for a line that is parallel to this line and crosses the  $y$ -axis at 4.
- B. Write an equation for a line that is perpendicular to this line and crosses the  $y$ -axis at -2.



## Lesson 3-3: Linear Combination Situations

### Vocabulary

Slope: \_\_\_\_\_

Slope = \_\_\_\_\_ OR \_\_\_\_\_

### Practice

1. In pro hockey, a win is worth 2 points, a tie is worth 1 point, and a loss is worth 0 points. Early in the season a team had 11 points.
  - A. Write a linear combination to express the relationship among the number of wins  $W$ , the number of ties  $T$ , and the number of losses  $L$ .
  - B. Make a table and graph of all possible  $(W, T)$  that could occur.
  
2. A chemist mixes  $x$  ounces of a 20% acid solution with  $y$  ounces of a 30% solution. The final mixture contains 9 ounces of acid.
  - A. Write a linear combination relation  $x$ ,  $y$ , and the total number of ounces of acid.
  - B. How many ounces of the 30% acid solution must be added to 2.7oz of the 20% solution to get 9oz of acid in the final mixture?

3. Find the slope given two points  $(-2, 3)$  and  $(4, 15)$ .

## Lesson: Intercepts

We already know how to find the \_\_\_\_\_ by looking at an equation in \_\_\_\_\_  
\_\_\_\_\_. Now, we are going to learn how to find the \_\_\_\_\_ & \_\_\_\_\_ intercepts from ANY form.

### Vocabulary

Intercept: \_\_\_\_\_  
\_\_\_\_\_

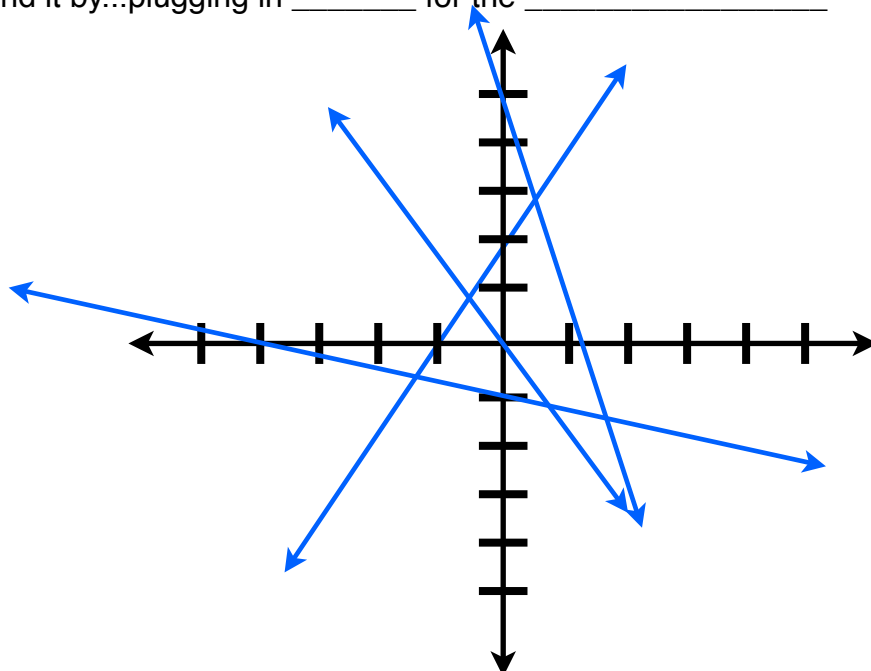
\*they are very useful in graphing, solving, and interpreting real-life situations!

x-intercept: \_\_\_\_\_  
\_\_\_\_\_

Find it by...plugging in \_\_\_\_\_ for the \_\_\_\_\_

y-intercept: \_\_\_\_\_  
\_\_\_\_\_

Find it by...plugging in \_\_\_\_\_ for the \_\_\_\_\_



## Practice

Find the  $x$  &  $y$  intercepts of each equation.

1.  $y = 2x - 3$

2.  $2x + 4y = 32$

3.  $y = -2$

## Lesson 3-4: Graphing in Standard Form

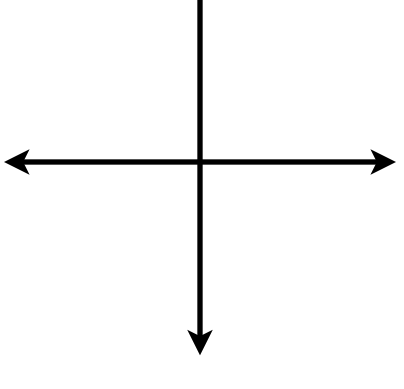
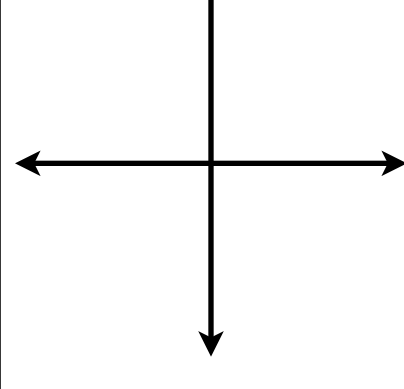
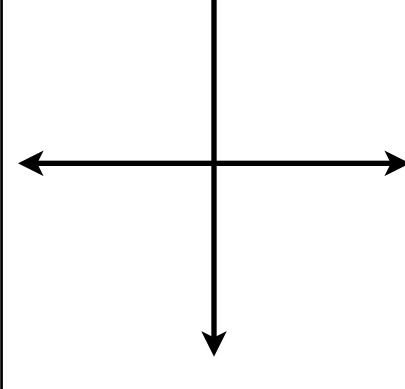
### Vocabulary

Remember, we already learned about slope-intercept form of a linear equation, but that is not the only form. We also have...

Standard Form: \_\_\_\_\_

- A, B, and C are all \_\_\_\_\_ (no fractions or decimals!)
- It is easiest to graph from standard form using the \_\_\_\_\_

### TYPES OF LINES

Oblique Line	Vertical Line	Horizontal Line
		
Looks like...  or...  Slope =	Looks like...  Slope =	Looks like...  Slope =

## Practice

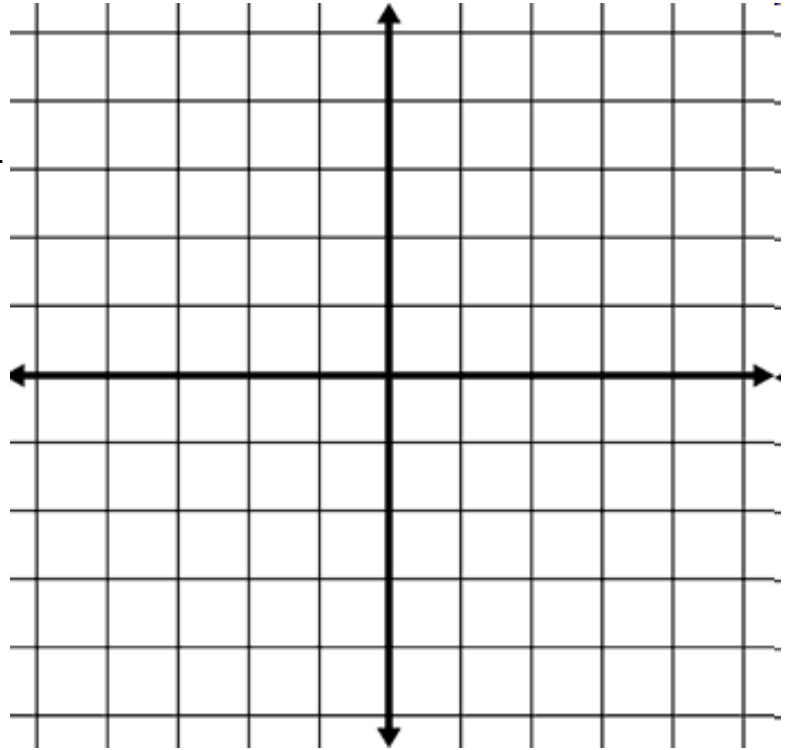
1. Using the equation  $0.2x + 0.3y = 9$ .

### STEPS:

1. Find the intercepts.
2. Plot the intercepts & connect with a straight line!

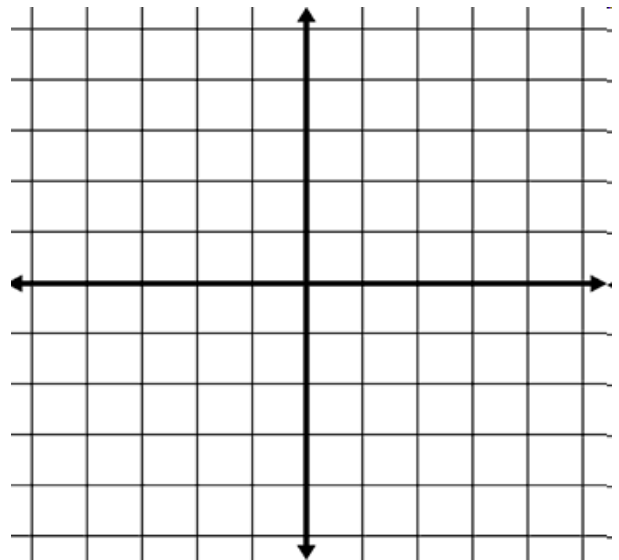
x-intercept:

y-intercept:

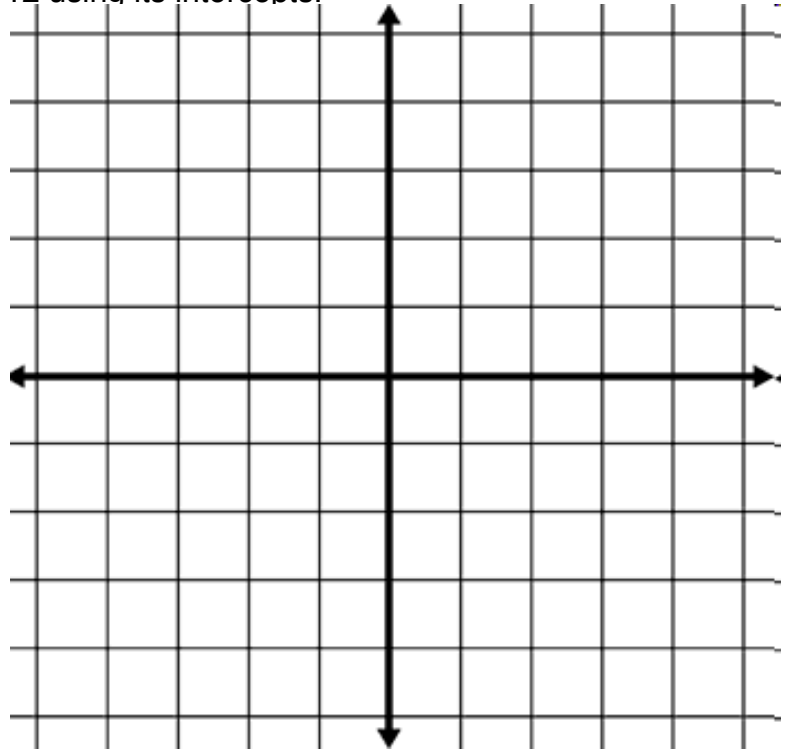


2. A. Graph the line  $x = 2$ .

B. Find the slope of the line.



2. Graph the equation  $6x - 3y = 12$  using its intercepts.



## Lesson 3-5: Writing the Equation for a Line

### Vocabulary

When possible, use \_\_\_\_\_! You only need two pieces of information...

### Practice

1. slope = -3, y-intercept = 2 Equation: \_\_\_\_\_
2. slope =  $\frac{1}{2}$ , y-intercept = -5 Equation: \_\_\_\_\_
3. slope = 0, y-intercept = -3.5 Equation: \_\_\_\_\_
4. slope = -4, y-intercept = 0 Equation: \_\_\_\_\_

**BUT WAIT!!!** What if you don't know the slope?!?! Then...\_\_\_\_\_!

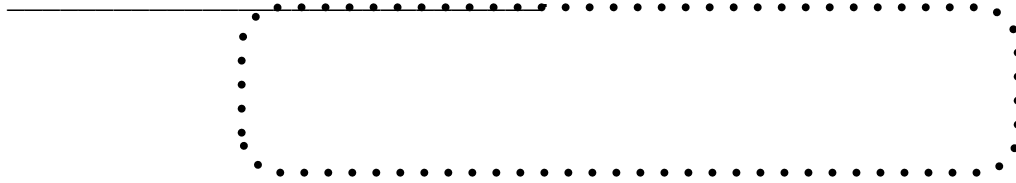
### Practice

5. Contains points (-2, 3) & (6, -1); y-intercept = 2.  
Equation: \_\_\_\_\_
6. Contains points (7, 3); y-intercept = 5.  
Equation: \_\_\_\_\_
7. Contains points (-2, 4) & (0, 12).  
Equation: \_\_\_\_\_



**BUT WAIT!!!** What if you don't know the  $y$ -intercept?!?! That's a little different...

When you don't know the  $y$ -intercept, you can use a new form called



We can work from point-slope form to find \_\_\_\_\_!

### **Practice**

8. Find the equation of a line with slope = 3, passing through point  $(-2, 10)$ .

9. Find the equation of a line through point  $(3, 5)$  and  $(6, -1)$ .

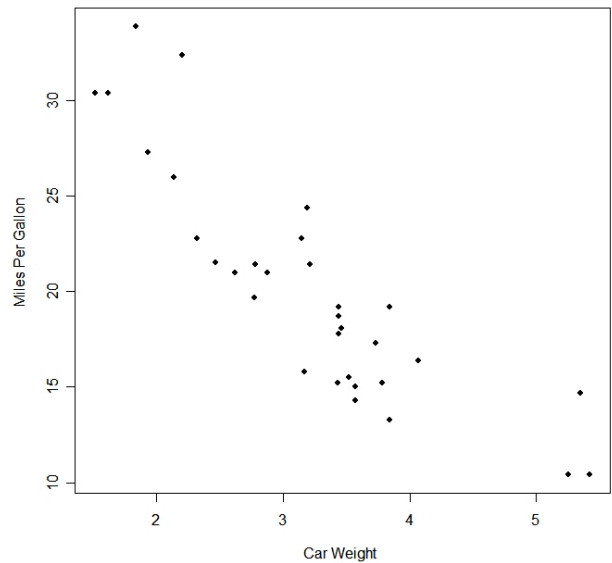
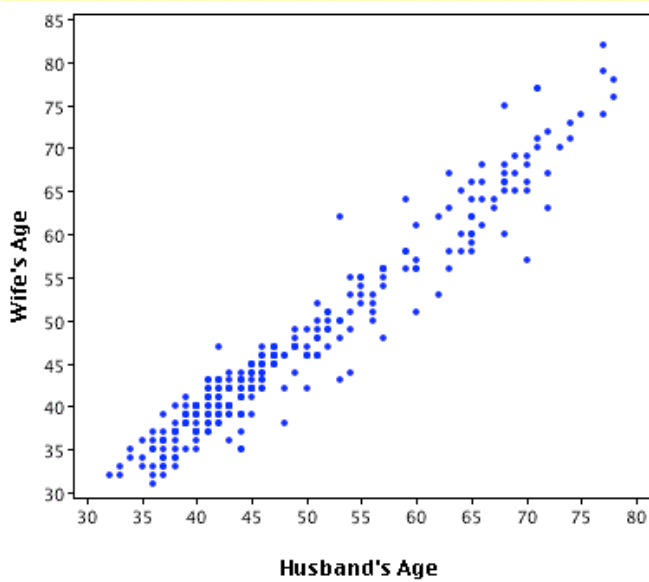
# Lesson 3-6: Linear Regression

## Vocabulary

Scatterplot: \_\_\_\_\_

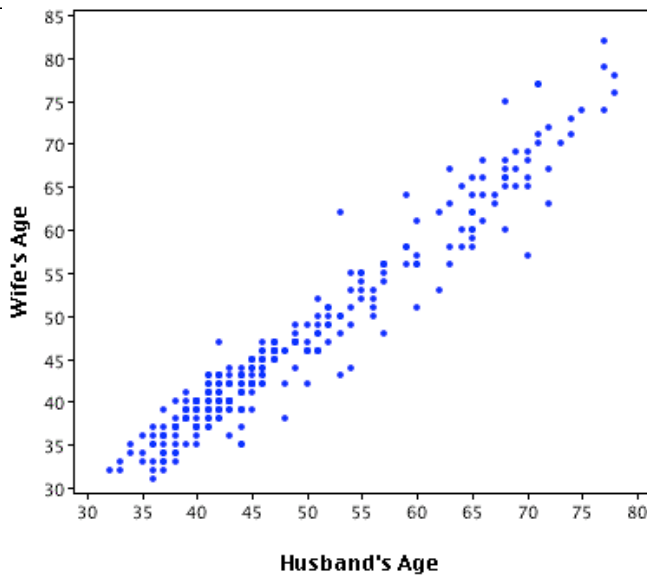
- Data is \_\_\_\_\_
- Data is usually collected from an experiment of some type of \_\_\_\_\_

Scatterplot Example



Line of Best-Fit/Line of Regression: \_\_\_\_\_

Example



**\*useful for making predictions with data**

Correlation: \_\_\_\_\_

**Positive Correlation** means that as one quantity \_\_\_\_\_, the other \_\_\_\_\_ as well.

**Negative Correlation** means that as one quantity \_\_\_\_\_, the other \_\_\_\_\_.

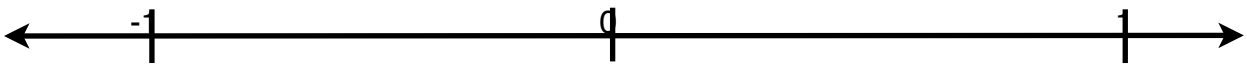
\*\*\*NOTE: Correlation does NOT imply \_\_\_\_\_!!! Just because two variables are correlated, does NOT mean that one is causing the other!

Correlation Coefficient ( $r$ ): \_\_\_\_\_

If  $r$  is positive, the correlation is \_\_\_\_\_ & the slope of the line is \_\_\_\_\_.

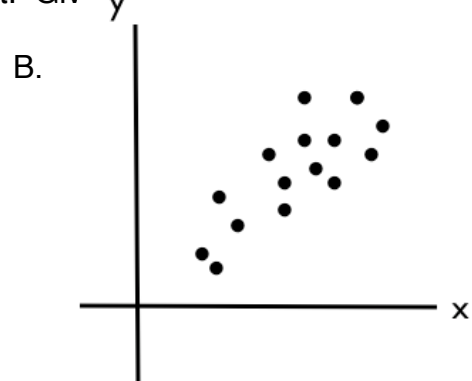
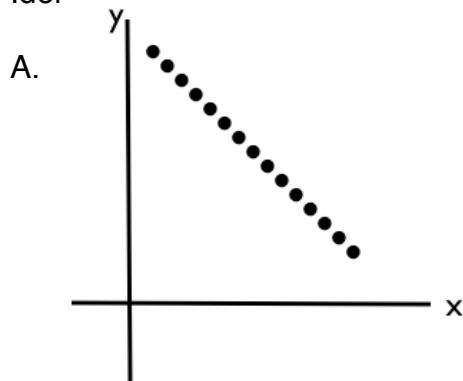
If  $r$  is negative, the correlation is \_\_\_\_\_ & the slope of the line is \_\_\_\_\_.

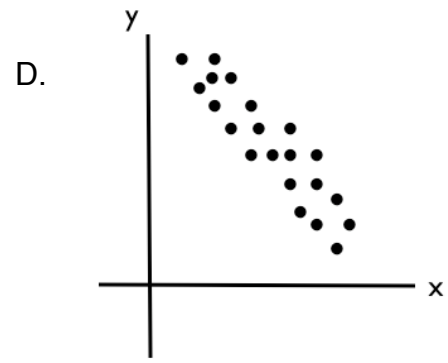
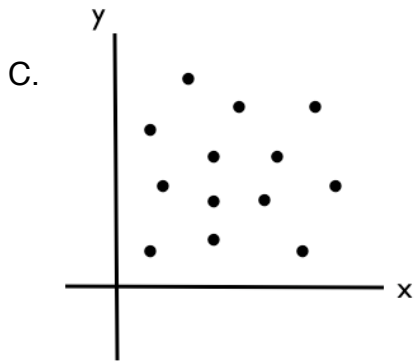
The **absolute value of  $r$**  indicates the \_\_\_\_\_ of the correlation or linear relationship. The closer the magnitude of  $r$  is to 1, the stronger the linear relationship.



## Practice

1. Identify the type of correlation for each data set. Give an approximate value for  $r$ .





2. Find the line of best-fit that represents the data below. Interpret the slope in context.

# of Absences	0	1	2	3	4	5	6	7	8
Avg. Grade	92	90	83	76	72	68	60	54	50

3. Find the line of best-fit that represents the data below. Interpret the slope in context.

# of siblings	0	1	2	3	4
Avg. Grade	78	84	86	76	80